Advances in multiagent simulation techniques have made possible the study of realistic highway traffic patterns and have allowed theories based on driver behaviour to be tested. Such simulations display various empirical features of traffic flows, and are used to design traffic controls that maximize the throughput of vehicles on busy highways. In addition to its intrinsic economic value, vehicular traffic is of interest because it may be relevant to social phenomena in which diverse individuals compete with each other under certain constraints. Here we report simulations of heterogeneous traffic which demonstrate that cooperative, coherent states can arise from competitive interactions between vehicles. As the density of vehicles increases, their interactions cause a transition into a highly correlated state in which all vehicles move with approximately the same speed, analogous to the motion of a solid block. This state is safer because it has a reduced lane-changing rate, and the traffic flow is high and stable. The coherent state disappears when the vehicle density exceeds a critical value. We observe the effect also in real traffic data.

In many social situations, decisions made by individuals lead to external effects that may be very regular, even without a global coordinator. In traffic, these decisions concern when to accelerate or brake, to overtake or to enter a busy multi-lane road, while trying to get ahead as fast as possible, but safely, under the constraints imposed by physical limitations and traffic rules. At times these behaviours give rise to very regular traffic patterns, as exemplified by the universal characteristics of moving traffic-jam fronts or synchronized congested traffic. These phenomena are in contrast with usual social dilemmas, where cooperation in order to achieve a desirable collective behaviour hinges on having small groups or long time horizons.

Here we describe a type of collective behaviour that we discovered when studying the dynamics of a diverse set of vehicles, such as cars and lorries, travelling along a two-lane highway with different velocities. As the density of vehicles in the road increases, there is a transition into a highly coherent state characterized by all vehicles having the same average velocity and a very small dispersion around this value. The transition to this behaviour becomes apparent when looking at the travel-time distributions of cars and lorries, comprising the overall dynamics on a stretch of highway. These travel times were obtained by running computer simulations using a discretized follow-the-leader algorithm, which distinguishes two neighbouring lanes of a unidirectional highway. Both are subdivided into sites \( z \in \{1, 2, \ldots, L \} \) of equal length \( \Delta x = 2.5 \text{ m} \). Each site is either empty or occupied, the latter case representing the back of a vehicle of type \( a \) (for example, a car or a lorry) with velocity \( v = \alpha u \Delta x \). Here \( u \in \{0, 1, \ldots, u_{max} \} \) is the number of sites that the vehicle moves per update step \( \Delta t = 1 \text{ s} \). Cars and lorries are characterized by different ‘optimal’ or ‘desired’ (that is, maximally safe) velocities \( U_a(d_a) \) with which the vehicles would like to drive at a distance \( d_a \) to the vehicle in front (see symbols in Fig. 2). Their lengths \( l_a \) correspond to the maximum distances satisfying \( U_a(l_a) = 0 \). At times \( T \in \{1, 2, \ldots, \} \), that is, every time step \( \Delta t \), the positions \( z(T) \), velocities \( u(T) \) and lanes \( l(T) \) of all vehicles are updated in parallel. We have ruled out simulation artefacts by this update method, which is appropriate for flow simulations.

Denoting the position, velocity and distance of the respective leading vehicle (+) or following vehicle (−) on lane \( i(T) \) by \( z_i, u_i \) and \( d_i = |z_i - z| \), in the adjacent lane by \( z_i', u_i' \) and \( d_i' = |z_i' - z| \), the successive update steps are:

1. Determine the potential velocities \( u(T + 1) \) and \( u'(T + 1) \) on the present and the adjacent lane according to the acceleration law

\[
\frac{u'}{u}(T + 1) = \frac{L}{U_a(d_i')} + (1 - \lambda)u(T)
\]

where the floor function \( [x] \) is defined by the largest integer \( l \leq x \). This describes the typical follow-the-leader behaviour of driver-vehicle units. Delayed by the reaction time \( \Delta t \), they tend to move with their desired velocity \( U_{sa} \) but the adaptation takes a certain time \( \tau = \lambda \Delta t \) because of the vehicle's inertia.

2. Change lane in accordance with, for simplicity, symmetrical (‘American’) rules, if the following incentive and safety criteria are fulfilled: check if the distance \( d_i' - T \) to the following vehicle in the neighbouring lane is greater than the distance \( u(T + 1) \) that this vehicle is expected to move within the reaction time \( \Delta t \) (safety criterion 1). If so, the difference \( D = d_i' - T - u(T + 1) > 0 \) defines the backward surplus gap. Next, look if you could go faster in the adjacent lane (incentive criterion). Finally, make sure that the relative velocity \( [u(T + 1) - u'(T + 1)] \) would not be

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larger than $D + m$ (safety criterion 2), where the magnitude of the parameter $m \geq 0$ is a measure of how aggressive drivers are in overtaking (by possibly enforcing deceleration manoeuvres).

3. If, in the updated lane $i(T + 1)$, the corresponding potential velocity $u(T + 1)$ or $u'(T + 1)$ is positive, diminish it by 1 with probability $p$ in order to account for delayed adaptation and the variation of vehicle velocities.

4. Update the vehicle position according to the equation of motion $z(T + 1) = z(T) + u(T + 1)$.

Despite its simplifications, this model is in good agreement with the empirical known features of traffic flows, and it can be well calibrated. $x$ and $U_i(d_i)$ determine the approximate velocity-density relation and the instability region. The typical outflow from traffic jams and their characteristic dissolution velocity $\Delta u$ can be enforced by $\Delta t$ and $\Delta x$. The average distance between successive traffic jams increases with smaller $p$. The parameter $m$ allows us to calibrate the lane-changing rates. Our simulations started with uniform distances among the vehicles and their associated desired velocities. The lorries were randomly selected. As our evaluations started after a transient period of one hour and extended over another four hours, the results are largely independent of the initial conditions.

Investigating the density-dependent average velocities of cars and lorries yields further insight into the solid-like state (Fig. 2). For small $p$ one finds that, at a certain ‘critical’ density, the average speed of cars decays significantly towards the speed of the lorries, which is still close to their maximum velocity. At this density, the highway space is almost used up by the safe vehicle distances, so that sufficiently large gaps for lane-changing can only occur for strongly varying vehicle velocities (like for large $p$). However, because the speeds of cars and lorries are almost identical in the solid-like state, the lane-changing rate drops by almost one order of magnitude (Fig. 3). Consequently, without opportunities for overtaking, all vehicles have to move coherently at the speed of the lorries, which closes the feedback loop that causes the transition. The solid-like flow does

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**Figure 2** Numerically determined average velocities of cars (solid lines) and lorries (short-dashed lines) as a function of the overall vehicle density. **a.** Two transitions are observed. 1. Up to a density of 24 vehicles per km, the average velocity of lorries remains unchanged. This is analogous to the dynamics of mixed one-lane traffic because of their slower speed, lorries experience smaller local densities as long as the average velocity of pure car traffic (crosses) stays above the maximum velocity of lorries, so that the road is not completely used by the vehicular space requirements at this speed. Then, the average lorry speed falls significantly with growing density to maintain safe vehicle distances. This causes an instability of traffic flow, resulting in a formation of stop-and-go traffic. 2. At a density of ~21.5 vehicles per km, the average velocity of cars drops almost to the average velocity of lorries, which leads to a distinct minimum in the difference of both curves (long-dashed line). This transition seems to be quite sharp, as illustrated by the inset at greater density resolution. Between 21.5 and 24 vehicles per km, the vehicles move like a solid block. Obviously, this is not enforced by the difference between the assumed dependencies of the desired velocities of cars (diamonds) and lorries (squares) on the local density ahead of them, defined by the inverse vehicle distance. The parameter values were chosen as in Fig. 1, but the observed effects are not very sensitive to the particular choice. Different values of $m$ give the same qualitative results (b). A higher proportion of lorries leads to an earlier transition to solid-like behaviour. Increasing the fluctuation parameter $p$ causes a smoother, but still visible, transition, until it disappears for $p = 0.3$ (c). A similar effect occurs for the width of velocity or parameter distributions characterizing cars and lorries.

**Figure 3** Dependence of desired and actual lane-changing rates and associated quantities on the overall vehicle density. a. The simulated actual lane-changing rates break down in the density range of coherent motion. Here, the parameters are the same as in Figs 1 and 2. For stronger fluctuations $p$, the minimum is less pronounced, but still noticeable up to $p < 0.3$. Smaller values of $m$ reduce the number of lane changes, but do not prevent the solid-like state. We have checked whether the lane-changing rate breaks down because, with identical velocities of cars and lorries in both lanes, there may be no advantage to lane changing. However, if the rates of desired lane changes (according to the incentive criterion) are reduced at all, they still keep a high level. b. The transition point around 21.5 vehicles per km is characterized by a rapid decay of the proportion of successful lane changes (that is the quotient between actual and desired lane changes). c. With growing density, not only the average of the gaps in front of cars decreases (squares), but also their standard deviation (diamonds). Opportunities for lane-changing are rapidly diminished when gaps of about twice the safe vehicle distance required for lane-changing cease to exist. This relates to a significantly smaller slope of the gaps’ standard deviation after the solid-block transition (broken lines; $k$ denotes the density per lane). The breakdown of the lane-changing rate seems to imply a decoupling of the lanes, that is, an effective one-lane behaviour. However, this is already the result of a self-organization process based on two-lane interactions, as any significant perturbation of the solid-block state (such as different densities in neighbouring lanes or velocity variations) will cause frequent lane changes. By filling large gaps, the gap distribution is considerably modified (also compared to mixed one-lane traffic). This will eventually reduce possibilities for lane changes, so that the solid-like state is restored.
not change by adding vehicles until the whole highway is saturated by the vehicular space requirements at the speed of the lorries. Then, the vehicle speeds decay significantly to maintain safe vehicle distances. The onset of stop-and-go traffic at this density produces gaps that vary by a large amount, so that overtaking is again possible and the coherent state is destroyed. For large $p$, we do not have a breakdown of the lane-changing rate at the critical density and, hence, no coherent state. Nevertheless, lane-changing cars begin to interfere with the lorries, so that the average velocity of lorries starts to decrease with growing density before the average car velocity comes particularly close to it (Fig. 2c).

As shown in Fig. 4, our prediction of the transition into a coherent state is supported by empirical data obtained from highway traffic in the Netherlands. Clearly, the difference between the average velocities of cars and lorries shows the predicted minimum at a density around 25 vehicles per kilometre and lane, where the average car velocity approaches the constant velocity of the lorries (Fig. 4a, b). The fact that the empirically observed minimum is less distinct than in Fig. 2a can be reproduced by higher values of the fluctuation parameter ($p \approx 0.15$) and points to a noisy transition. This interpretation is also supported by the relative fluctuation of vehicle speeds (Fig. 4c), which shows a minimum at the same density, while remaining finite. A similar result is obtained for the interaction rates of vehicles (Fig. 4d).

We have presented here a new effect in highway traffic that consists of the formation of coherent motion out of a disorganized vehicle flow by competitive interactions. The predicted solid-like state is supported by real highway data, and our interpretation of the effect suggests that it is largely independent of the chosen driver-vehicle model (although the transition may be less sharp in a continuous model). It would be interesting to see if the spontaneous appearance of coherent states is also found in other social or biological systems, such as pedestrian crowds, cell colonies or animal swarms.

We note that the coherent state of vehicle motion considerably reduces the main sources of highway accidents: differences in vehicle speeds and lane-changes. It is also associated with maximum throughput in the highway, and is located just before the transition to unstable traffic flow. Thus, at a practical level it is desirable to implement traffic rules and design highway controls that are aimed to make traffic’s moving like a solid block. Close to the transition point, the formation of this coherent state could be supported by traffic-dependent lane-changing restrictions and variable speed limits or by automatic vehicle control systems. Compared with ‘American’ (symmetric) lane-changing rules, ‘European’ rules seem to be less efficient: an asymmetric lane usage, where lorries mainly keep in one lane and overtaking is carried out in the other lane(s), motivates car drivers to avoid the lorry lane, so that the effective highway capacity is reduced by up to 25%.

Received 30 April, accepted 16 September 1998.

Figure 4 Mean values of one-minute averages that were determined from single-vehicle data on mixed traffic on the Dutch two-lane highway A9 on 14 subsequent days. Panels a and b depict the density-dependent average velocities of cars (solid lines) and lorries (short-dashed lines) in the right and left lane, respectively. Their differences (long-dashed lines) show the predicted minimum at densities of ~25 vehicles per km, up to which the velocity of lorries is almost constant. c. The relative fluctuations of car speeds (defined as velocity variance divided by the square of average velocity) display minima at the same densities, which points to a more coherent motion in the car fraction. d. The interaction rates per vehicle also show a minimum around 25 vehicles per km. This corresponds to a decreased relative velocity among successive vehicles. The interaction rate is defined by the average of min($\Delta v(\Delta t, 0)$), where $\Delta v$ denotes the velocity difference to the vehicle in front. We point out that the above data support the predictions of our model despite its simplifications. In particular, this concerns the asymmetry of European lane-changing rules, which imply that overtaking is allowed only in the left lane, but vehicles should switch back to the right lane as soon as possible. At least at velocities of $<80\,\text{km\,h}^{-1}$ vehicles also pass in the right lane with small relative velocities to vehicles in the left lane. Nevertheless, the rate of lane changes from and to each lane is, on average, the same. One result of the mentioned asymmetry, however, is a smaller fraction of lorries in the left lane, which diminishes the related minimum in c. Another consequence is the tendency to have a higher average car velocity in the left lane, so that in b, compared to a, the minimum in the difference between the average speeds of cars and lorries is more pronounced.


Acknowledgements. D.H. thanks the DFG for support by a Heisenberg scholarship, and H. Täule and the Dutch Ministry of Transport, Public Works and Water Management for supplying the highway data, which were evaluated by V. Shvetsov.

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